

# Model Residual Stress by Finite Element Method

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*Abstract:* - This paper presents an original model developed by finite element method to simulate the behavior of the material to the method "Blind Hole Drilling", to determine the residual stress. Modeling of this method is possible through the use of the "Birth and Death" which have some elements of ANSYS library. After obtaining the analysis of movements, appropriate loads, a node located from the center hole at a radius calculated. In this way it is easier to estimate the stresses and deformations of a piece. Several measurements are made and based on this model is given in ANSYS. In this way we can have a map of tensions and deformations in a material..

*Key-Words:* - residual stress, method "Blind Hole Drilling", welded constructions

## 1 Introduction

One of the most common methods of residual stress measurement technique is the method " Blind Hole Drilling " .

Under this method, after installing the piece of sensors (strain gauges) is practiced shallow hole and surface modification state of deformation measured in the vicinity of the hole. From experimental data obtained can be calculated residual stresses relaxed (released). This method is considered semi - destructive as long as the small hole in most cases not significantly affect the structural integrity of the part being tested. It is a typical hole  $D_0 = 1/16" = 1,5\text{mm}$  and  $D_0 = 1/8" = 3,0\text{mm}$  both in depth and diameter. If necessary, the hole can be covered after measurement. This is a standard test method, developed by the American Society for Testing and Materials (ASTM 837). Figure 1 shows the drilling device RS-200 model.



Fig. 1. End-Mill Drilling RS-200 model.

## 2 Principle of the method "Blind Hole Drilling"

Practice of hole (even very small diameter) in a body residual stress, relax tension in that place because the normal stress at any free surface (in this case the surface hole) must necessarily be zero. Elimination normal stress at the edge of the hole reduce tensions in the region surrounding vicinity, causing local deformations to be amended accordingly. Measuring strain changes caused by stress relaxation provides the necessary data for calculation. When you take avery small hole diameter (fig.2) in a region containing residual stresses, deformations sizes at point P are functions of the main local stress  $\sigma_p$  and  $\sigma_q$  and the geometric relationship between point and hole between point and principal axes.

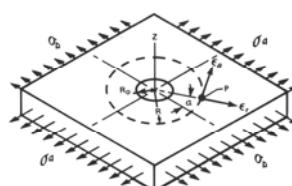


Fig. 2. Strain relaxation at point "P" due to a hole practice.

For example, if one considers deformations of the point where the main stressis present only  $\sigma_p$ , then we can write the relations:

$$\varepsilon_r = -\sigma_p \frac{1+\nu}{2E} \left[ \frac{1}{r^2} - \frac{3}{r^4} \cos 2\alpha + \left( \frac{4}{1+\nu} \right) \frac{1}{r^2} \cos 2\alpha \right] \quad (1)$$

$$\varepsilon_\theta = -\sigma_p \frac{1+\nu}{2E} \left[ -\frac{1}{r^2} + \frac{3}{r^4} \cos 2\alpha - \left( \frac{4\nu}{1+\nu} \right) \frac{1}{r^2} \cos 2\alpha \right] \quad (2)$$

$$\gamma_{r\theta} = \frac{\sigma_p}{2G} \left( \frac{3}{r^4} - \frac{2}{r^2} \right) \sin 2\alpha \quad (3)$$

$$\varepsilon_r - \varepsilon_\theta = -\sigma_p \frac{1+\nu}{2E} \left( \frac{2}{r^2} - \frac{6}{r^4} \cos 2\alpha + \frac{4}{r^2} \cos 2\alpha \right) \quad (4)$$

where:  $\varepsilon_r$ ,  $\varepsilon_\theta$  are tangential or radial deformations at point P;  $\gamma_{r\theta}$  - shear strain at point P,  $r=R/R_0$  dimensionless distance from the hole center point P, E, G,  $\nu$  - module of elasticity, transverse and Poisson coefficient of the material. Deformations revealed relationships expressed above are shown in figure 3 for  $\alpha = 0^\circ$  and  $\gamma = 90^\circ$  to illustrate their variation on the main axes directions in relation to the distance (dimensionless) from the center hole.

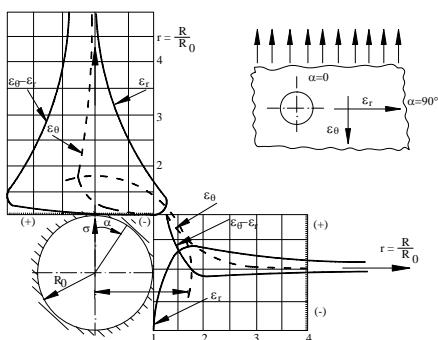


Fig. 3. Changes highlighted strains distance from the hole center (along-axis) - uniaxial residual stress.

As the distance from the hole increases, deformations decline rapidly. For this reason, to obtain a maximum signal strain gauges, it is preferable that the measurement be made as close to the hole. On the other hand, increasing parasitic effects in the immediate vicinity of the hole. These considerations lead to the understanding of compromise in selecting the optimal range.

As shown in figure 4 is installed three rosette strain gauges oriented radially to the center of the radius R from the center hole. We recommend the use of specialized products rosettes "Micro-Measurements Division". Rosettes are available in two versions ( $R = 0.101\text{in}$ ,  $R = 0.202\text{in}$ ) with different types of temperature compensation.

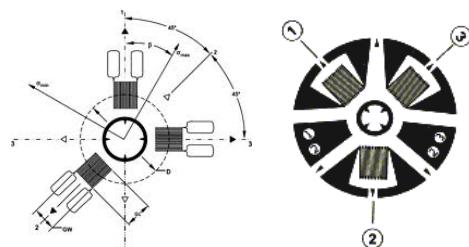


Fig. 4. Positioning rosette strain gauges for determining residual stress.

### 3 Modeling by finite element method "Blind Hole Drilling"

Finite element modelling method "Blind Hole Drilling" for determining residual stress a material can be done using the feature "Birth and Death" (activation-deactivation), which have some elements of ANSYS meshing the library.

The "Birth and Death" every element mesh is used to activate and deactivate them when material is added (or removed) from the system. Thus, some elements of the modelling "existing" or "absent". To achieve the "element death" ANSYS program does not remove disabled items but to reduce stiffness. Although the loads associated disabled elements are brought to zero, they appear in the list of elemental charges.

#### 3.1 Creating model

Design geometry model begins by building a parallelepiped with dimensions of  $10 \times 10 \times 4\text{mm}$ . Within this volume are defined six volumes rectangular cylinder diameter and total depth of 3mm (fig. 5a).

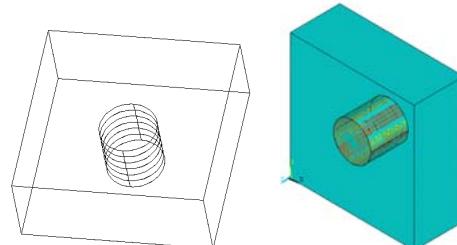


Fig.5.a Creating volumes.

Subsequently, these six volumes elements are assigned properties "Birth and Death" so that it can be modelled and incremental "Blind Hole Drilling" method. Inside this volume are defined rectangular cylindrical diameter and six volumes total depth of 3mm (Fig.5 b).

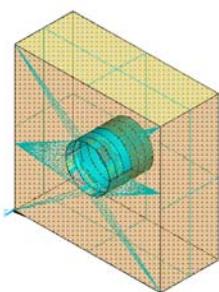


Fig.5b. Six cylindrical volume to be removed successively-incremental method.

Meshing volumes (fig.6) using SOLID92 element determines obtain items totalling 16,989 nodes.

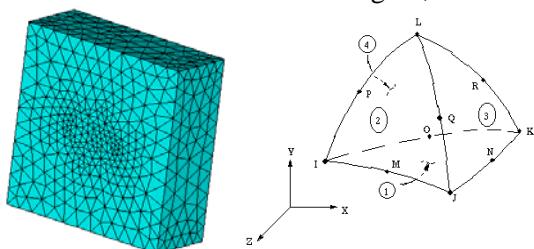


Fig. 6. Mesh elements parallelepiped volumes (SOLID 92).

In table 1 is indicated the number of cylindrical volumes, the depth and the relevant elements.

Table 1. Hole depth and volume elements.

No.volume	Depth [mm]	Elements
1	0,5	1-531
2	0,1	532-1107
3	1,5	1108-1676
4	2,0	1677-2245
5	2,5	2246-2815
6	3,0	2816-3389

### 3.2 Application loading

Choose the type of static analysis. For induction into the fabric of a state of biaxial tension flat areas apply lateral load displacement type (fig.7) with values between 0.01-0.1mm in six steps(0.01, 0.025, 0.05, 0.075, 0.1mm). The solution runs through seven successive runs. The first run does not disable any corresponding element cylindrical volumes. For

each of the six following analysis is off by a volume cylindrical elements.

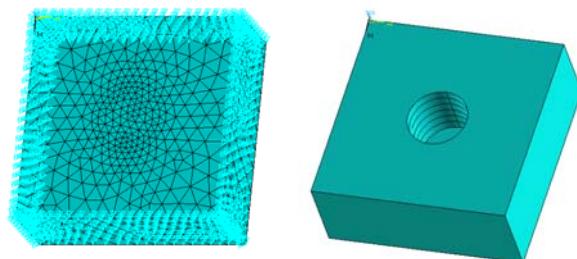


Fig.7. Application loading and off elements.

In figure 8 are represented three of the six off successive phases corresponding cylindrical hole data volumes incremental material.

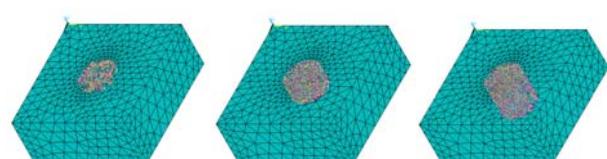


Fig. 8. Disabling successive elements of the six volumes of hole.

Finite element modelling method "Blind Hole Drilling", to determine the residual stress in a material seeking a node displacements values found on the material at a radius calculated according to the theory of strength of materials by  $R_{ph}= 2,598$  mm from the center hole. For this purpose (fig.9), select the area on the surface of box volume (Area 41), which is measuring the deformations that occur increasing tensions by playing the hole (in a single pass at a depth equal to the diameter of the hole or incremental). In this area, choose a node (Node 6192) located at the radius corresponding to the calculated (2.598mm). The tables with the results calculated by the processor selects the direction OX nodal displacement values corresponding to this node.

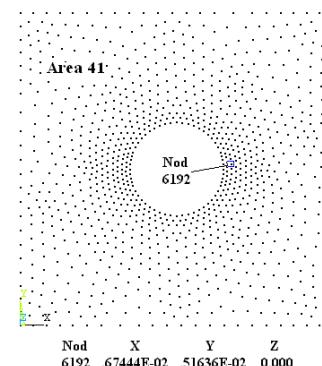


Fig.9. Selecting Node 6192 on Area 41.

The results displacements for node 6192 adequate to loads applied displacement volume of rectangular side areas that will induce tension are given in table 2.

Table 2. Nodal displacement values.

Displacement load ( $\pm UX$ )/( $\pm UY$ ) [mm]	Displacement UX nod.6192 [mm]
1 E-02	0.0076839
2.5 E-02	0.0019258
5 E-02	0.0038677
7.5 E-02	0.0058258
10 E-02	0.0078001

Graphical representation of the load-displacement pairs of values shows a very good linearity. Using a spreadsheet program is determined linear equation (fig10).

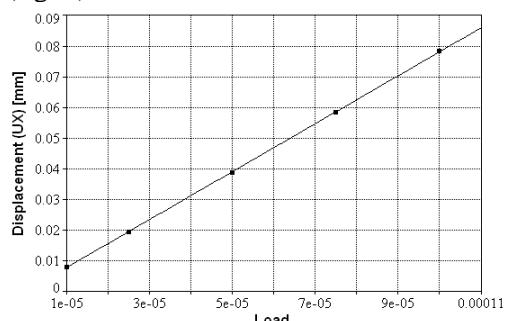


Fig. 10. Dependency relationship load - displacement.

Results strains (von Misses and Intensity) for node 6192, in order deactivation of successive volumes of the six corresponding hole until it reaches a depth value equal to its diameter are given in table 3.

Table 3 Values corresponding deformations volumes off

Deactivated volume	Node no.	Von Misses strain	Intensity strain
0	0	0.009402	0.00942
1	1-531	0.011446	0.011604
2	532-1107	0.013074	0.013863
3	1108-1676	0.014003	0.015041
4	1677-2245	0.014507	0.015504
5	2246-2815	0.014623	0.015564
6	2816-3389	0.014537	0.015554

Figure11 is plotted the variation deformation (von Misses and Intensity) for node 6192, using the data from table 3.

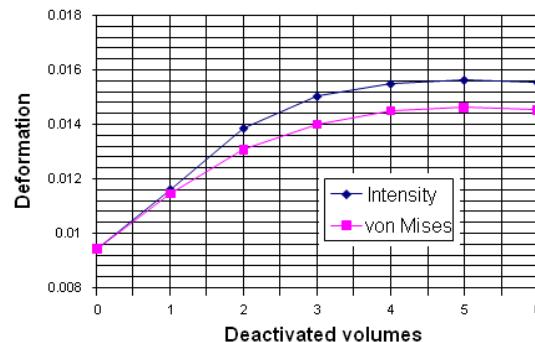


Fig. 11. Variation of deformation (von Mises and Intensity) with volume off.

In figure 12 are plotted nodal results, von Mises-section deformations resulting from successive runs that was disabled by a volume of the hole, thus simulating method "Blind Hole Drilling" incremental.

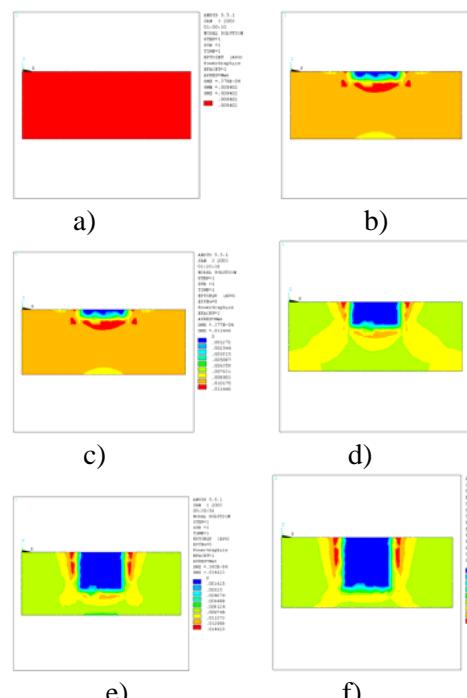


Fig.12. Representation of nodal results, vonMises strain-section for off successive volumes of the cylindrical hole.

To confront the results obtained from finite element modelling "Blind Hole Drilling" method with values derived from the methodology of calculation was calculated the percentage ratio of strain to the ratio depth/diameter ( $Z/D$ ) equal to off successive volumes the cylindrical hole. Results are shown in table 4.

**Table 4**

Deactivated volume	Z/D	Von Mises strain	Percentage ratio of strain	
			Strain difference	%
0	0	0.009402	0	0
1	0.166	0.011446	0.002044	39.149
2	0.333	0.013074	0.003672	70.331
3	0.5	0.014003	0.004601	88.125
4	0.666	0.014507	0.005105	97.778
5	0.833	0.014623	0.005221	100
6	1.0	0.014537	0.005135	98.353

Graphical representation of the values in Table 5 is given in Figure 13.

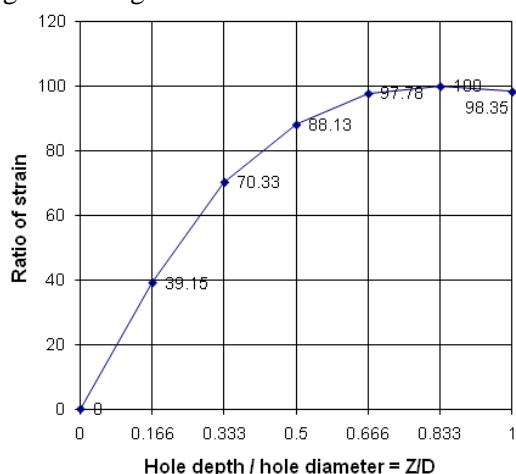


Fig.13. Ratio of strain to the ratio Z/D (depth/diameter)

#### 4 Conclusion

Presented an original model developed by finite element method that simulates the behaviour of the material to the method "Blind Hole Drilling", to determine the residual stress. Modelling of this method is possible through the use of the "Birth and Death" (activation-deactivation), which have some elements of ANSYS meshing library. To get the effect "element death", elements are cut off rigidity. After the analysis results are obtained displacements corresponding loads, a node located from the center hole at a radius calculated. To confront the results of modelling by Finite Elements Method, method "Blind Hole Drilling" with values from the calculation methodology calculated "the percentage strain ratio" the ratio depth/diameter, resulting in deactivation of successive volumes of the cylindrical hole. In industry, the percentage of use of welded constructions /welded parts is very high. After each welding cord we have strains and

deformations. Deformations are easy to see because they are visible and measurable. The state of stress in the material is determined more difficult and depending on the importance of the part, the thermal stress relief treatment is done or not. Thermal treatment involves some costs. It is necessary to know what is the level of tension in the material in the whole piece to make the decision to achieve or not the heat treatment of the piece. It is difficult to make hundreds of measurements on the same piece and therefore a finite element program can be used to simulate the residual stresses in the piece.

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