

# Effect of phosphorus addition on the MoS<sub>2</sub> phase morphology and performance of sulfided Mo/Al<sub>2</sub>O<sub>3</sub> catalysts in HDO of rapeseed oil

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**Abstract:** - The effect of phosphorus addition on the MoS<sub>2</sub> phase morphology and HDO activity was studied using catalysts, prepared without (MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst) or with the addition (P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst) of phosphoric acid to impregnation solution, initially containing MoO<sub>3</sub> and citric acid. Nearly the same average slab length of MoS<sub>2</sub> particles was determined with HRTEM on the surfaces of MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> and P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts. But the direct modeling of XRD patterns with using of the DSE gives the different average sizes of coherently scattering domains of the MoS<sub>2</sub> particles; with the lower  $d_{XRD}$  of the MoS<sub>2</sub> particles in the P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst. A lower value of  $d_{XRD}$  in the case of P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst seems to result from a higher degree of deformation of the supported MoS<sub>2</sub> particles, may be due to P incorporation in the MoS<sub>2</sub> slabs. Higher degree of deformation in turn could have been a reason of higher activity of P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst in HDO and HDS reactions.

**Key-Words:** - hydrodeoxygenation, hydrodesulfurization, hydrotreatment, MoS<sub>2</sub>, sulfide catalyst, co-processing, rapeseed oil

## 1 Introduction

The growing demand for transportation fuels along with the vital tendency to reduce the greenhouse gas emissions have stimulated the development of new catalysts for the production of liquid transportation fuels from the renewable resources. The hydroprocessing of triglyceride-based feedstock gives the mixture of alkanes, which are the valuable components for the improvement of the petroleum-based motor fuels properties [1]. The conventional hydrotreating sulphide CoMo/Al<sub>2</sub>O<sub>3</sub> or NiMo/Al<sub>2</sub>O<sub>3</sub> catalysts are widely used for the hydrodeoxygenation (HDO) of triglyceride-based feedstocks or their mixture with petroleum-derived fractions [2-10].

## 2 Problem Formulation

The HDO of triglycerides over sulfide Co(Ni)Mo/Al<sub>2</sub>O<sub>3</sub> catalysts proceeds through the deoxygenation (with the water formation) or via decarbonylation/decarboxylation (with COx production) pathways, the latter route is highly undesirable because of ecological and technological reasons [2,3]. The non-promoted sulfide Mo/Al<sub>2</sub>O<sub>3</sub> catalysts were shown to provide RSO conversion without considerable COx formation [11-13], that

makes them the promising candidates for the HDO of triglycerides. But the effects of precursors and preparation methods on the HDO activity were not studied in details. In our work the effect of phosphorus addition to the impregnation solution on the state of the active phase and the performance of MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts in HDO of rapeseed oil was investigated. Catalysts were prepared by an impregnation method with or without adding of phosphoric acid in the impregnation solution, prepared from MoO<sub>3</sub> and citric acid.

## 3 Problem Solution

### 3.1 Experimental

Mo/Al<sub>2</sub>O<sub>3</sub> catalysts was prepared by impregnation of alumina granules (BET surface area 208 m<sup>2</sup> g<sup>-1</sup>, pore volume 0.68 ml g<sup>-1</sup>, average pore diameter 13,2 nm, purchased by JSK "Promkataliz", Ryazan, Russia) with a two different aqueous solution. The first solution was prepared using MoO<sub>3</sub> and citric acid; the second one contained MoO<sub>3</sub>, citric acid and H<sub>3</sub>PO<sub>4</sub> (all purchased by Vekton, Russia). The samples were denoted as MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> and P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub>, respectively. The catalysts were dried

in nitrogen flow at room temperature and then at 110°C for 4 h.

The textural properties of the catalysts were determined using nitrogen physisorption with an ASAP 2400 instrument (USA); the elemental analysis was performed using Optima 4300 DV (Perkin Elmer, France). The morphology of sulfide phase was studied using a JEM-2010 electron microscope (JEOL, Japan) with 1.4 Å lattice resolution at a 200 kV accelerating potential. Prior to the study, the samples were ground, suspended in ethanol and placed on a copper grid coated with a holey carbon film. XRD investigations were carried out at an ARL X'TRA diffractometer (Thermo, Switzerland) with a Si(Li) solid-state detector and Cu K $\alpha$  radiation. The measurements were carried out in the 2 $\theta$  range of 10°-80° with a step of 0.1°. Phase analysis was performed using the ICDD PDF-2 database.

The catalytic experiments were performed in a trickle-bed down-flow reactor with an inner diameter of 16 mm and length of 570 mm. In each experiment 10 ml of catalyst was diluted by an inert material, carborundum (0.1–0.25 mm size fraction) in a 1:2 volume ratio. The catalysts were examined after sulfidation with straight-run diesel fraction containing additionally 0.6 wt. % sulfur as dimethyl disulfide (at H $_2$  pressure 3.5 MPa; H/C – 300 Nm $^3$ /m $^3$ ; LHSV- 2 hour $^{-1}$ ). The sulfidation was performed at 340°C during 6 h (heating rate was 25°C in hour). The catalytic experiments were performed at H $_2$  pressure 4.0 MPa, H/C – 600 Nm $^3$ /m $^3$ ; LHSV – 1.5 h $^{-1}$ , temperature – 260, 280, 300, 320 and 340°C; using mixture of 20 wt.% of rapeseed oil (RSO) diluted with straight run gas oil (SRGO). Properties of mixture were  $d = 0.86$  g/cm $^3$ , 2.34 wt. % O, 0.82 wt% S, 141 ppm N. The duration of each stages differing in temperature was 12 h; the residual sulfur and oxygen contents were obtained by averaging the data for three samples taken through 10, 11 and 12 h after the beginning of the current stage.

The sulfur content of the feedstock and that of the hydrogenated products were measured on a Lab-X 3500SCI energy dispersive X-ray fluorescence analyzer (Oxford Instruments, United Kingdom). The total oxygen content of the reaction mixture before and after hydrorefining was determined using a Vario EL Cube CHNSO analyzer (Elementar Analysensysteme GmbH, Germany).

The contents of C $_{18}$  and C $_{17}$  alkane (the products of RSO hydrodeoxygenation) in the products were evaluated using two-dimensional gas chromatography (Agilent 7890A GC equipped with

a flame-ionization detector and an Agilent flow modulator). In the first dimension, separation was fulfilled using helium as carrier gas and ZB-WAX capillary column of 25 m long with a diameter of 0.25 mm and the film thickness of 0.25  $\mu$ m (Phenomenex, United States). An HP-5 column of 5 m long and 0.25 mm in diameter with a film thickness of 0.25  $\mu$ m (Agilent, United States) was used for the separation of components in the second dimension. The carrier gas was hydrogen. The conditions of chromatography were 70°C for 0.5 min, 8°C/min, and 260°C for 25 min. The flow through the first column was 0.5 mL/min (helium), while the flow through the second column was 31 mL/min (hydrogen). The period of modulation was 2.2 s. The volume of the introduced sample was 0.5  $\mu$ L, and the split ratio was 1:200. The chromatographic data were processed with the ChemStation (Agilent) and Image GC (Zoex) software.

Gas phase was analyzed on-line using a gas chromatograph «Chromos 1000» (Dzerzhinsk, Russia), equipped with the FID detector. The concentrations of CO and CO $_2$  were determined in the form of methane after separation on column packed with 80/100 mesh HayeSep $^{\text{®}}$  («Sigma-Aldrich», St. Louis, MO, USA) and subsequent hydrogenation over reduced Pd catalyst at 340 °C.

### 3.2 Results and discussion

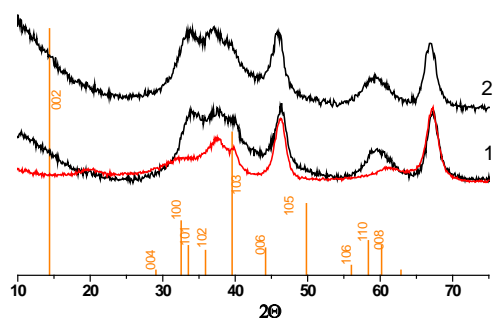
Powder X-ray diffraction (XRD) analysis and high-resolution transmission electron microscopy (HRTEM) were used to study the structure and dispersion of the supported MoS $_2$  particles in the sulfide catalysts.

Low degree of crystallization of MoS $_2$  in hydroprocessing catalysts is known to limit application of traditional XRD methods for structure diagnostics. The Debye Function Analysis (DFA) was used to extract information on the structure of MoS $_2$  nanoparticles from the XRD data. The Debye Scattering Equation (DSE) allows calculating XRD pattern of model nanoparticle with taking into account the particle shape, size, chemical composition, and atomic structure [14-17]. Calculating and fitting XRD patterns were performed using the DIANNA software [18]. To evaluate an agreement between the calculated and experimental XRD profiles, a profile discrepancy factor (R $_p$ ).

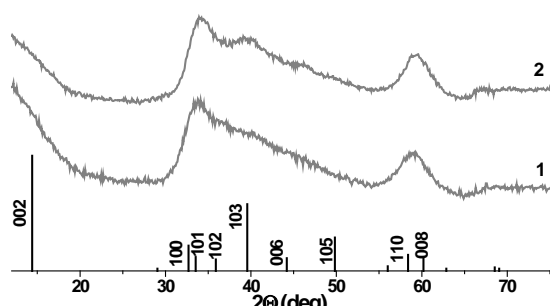
Fig.1 shows XRD patterns of the  $\gamma$ -Al $_2$ O $_3$  support and MoS $_2$ /  $\gamma$ -Al $_2$ O $_3$  catalysts. Highly broadened peaks in the 2 $\theta$  ranges of 33-35° and 58-60° were detected in the XRD patterns of the catalysts, which

indicate formation of highly dispersed MoS<sub>2</sub> phase. Overlapping of the diffraction lines corresponding to the MoS<sub>2</sub> and  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> phases complicates the analysis.

Difference curves between the normalized XRD patterns of the catalyst and support were obtained to extract structural information on the MoS<sub>2</sub> nanoparticles (Fig.2).



**Fig.1.** XRD patterns of the P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> (1) and MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> (2) catalysts in comparison with XRD pattern of the  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> support. The peaks of the MoS<sub>2</sub> phase are shown.

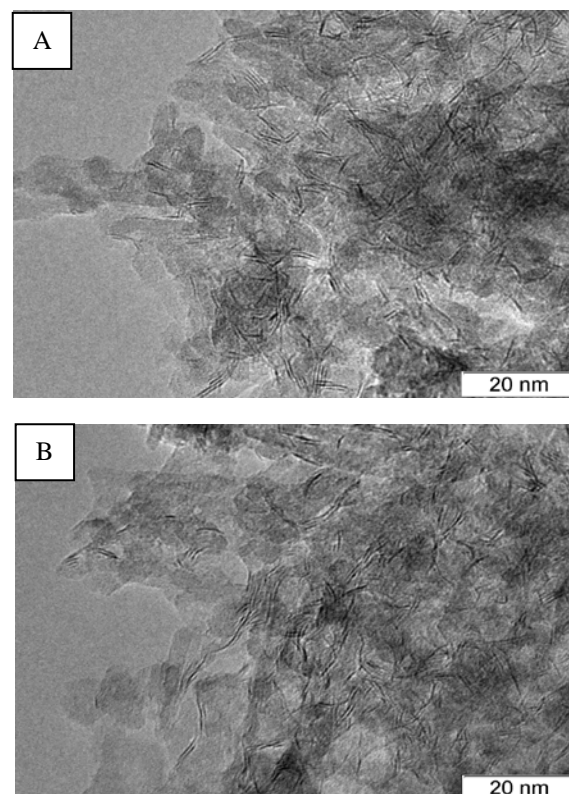


**Fig.2.** Difference XRD curves for the P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> (1) and MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> (2) catalysts

The formation of the poorly crystallized MoS<sub>2</sub> phase was revealed in the catalysts (JCPDS#37-1492,  $a=b=3.161$  Å,  $c=12.299$  Å,  $\alpha=\beta=90^\circ$ ,  $\gamma=120^\circ$ ). Disappearance of the first (002) reflection indicates the small size of coherently scattering domain ( $d_{\text{XRD}}$ ) in the [001] direction, in which the skeletal MoS<sub>2</sub> layers are packed. HRTEM data also gave evidence of poor crystallization of the MoS<sub>2</sub> particles along the [001] direction (Fig.3). The average stacking number of 1.6 was determined in the both P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> and MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts (Table 1).

A direct modeling of XRD patterns with using the DSE was performed to determine the average size of coherently scattering domain. Starting from

one MoS<sub>2</sub> unit cell, a set of model plate-like crystallites was generated by varying lengths of the crystallite edges. The simulation of XRD data confirmed the absence of significant MoS<sub>2</sub> stacking in the P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> and MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts.



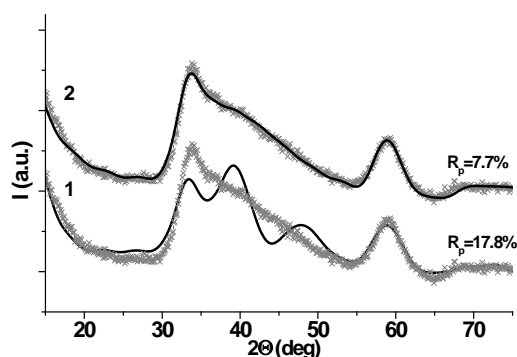
**Fig.3.** HRTEM images of the P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> (A) and MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> (B) catalysts

**Table 1.** Dispersion characteristics of MoS<sub>2</sub> particles in the sulfide catalysts from the XRD and HRTEM data

P-MoS <sub>2</sub> /Al <sub>2</sub> O <sub>3</sub>		MoS <sub>2</sub> /Al <sub>2</sub> O <sub>3</sub>	
average slab length of MoS <sub>2</sub> crystallites according to the XRD data modeling			
$d_{\text{XRD}}$ (nm)	$R_p$ (%)	$d_{\text{XRD}}$ (nm)	$R_p$ (%)
2.2x2.2	8.3	2.5x2.5	9.0
2.5x2.5	7.7	2.8x2.8	8.5
2.8x2.8	8.2	3.2x3.2	7.9
		3.5x3.5	7.8
		3.8x3.8	8.6
average slab length of MoS <sub>2</sub> particles according to the HRTEM data			
4.6		4.9	
average stacking number according to the HRTEM data			
1.6		1.6	

Fig.4 shows the experimental difference XRD curve of the P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst in comparison with

calculated XRD patterns for the plate-like  $\text{MoS}_2$  crystallites containing one and two  $\text{MoS}_2$  layers with lateral dimensions of  $2.5 \times 2.5$  nm ( $\text{MoS}_2$  crystallites composed of  $8 \times 8 \times 0.5$  and  $8 \times 8 \times 1$  unit cells, respectively).



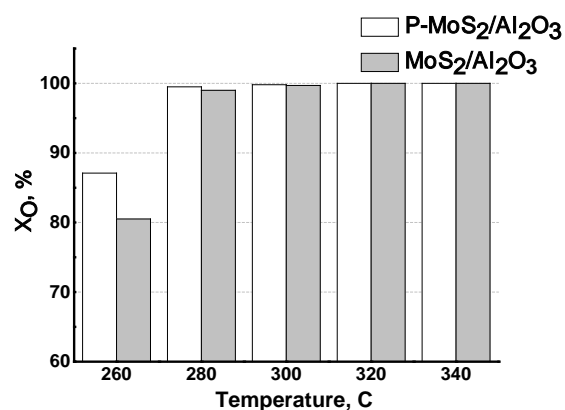
**Fig.4.** Experimental difference XRD curve of the P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalyst and calculated XRD patterns for  $\text{MoS}_2$  crystallites with dimensions of  $2.5 \times 2.5 \times 1.2$  nm (1) and  $2.5 \times 2.5 \times 0.6$  nm (2), containing one and two layers along the [001] direction, respectively.

The model of one-layer thick crystallites is more appropriate for describing the experimental XRD pattern. The calculated XRD pattern for the  $\text{MoS}_2$  crystallites composed of two layers differs drastically from the experimental one. The lateral dimensions of  $\text{MoS}_2$  crystallites of one-layer thickness (slab length) in the P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  and  $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalysts were refined. The sizes  $d_{\text{XRD}}$  and corresponding discrepancy factors  $R_p$  are listed in Table 1.

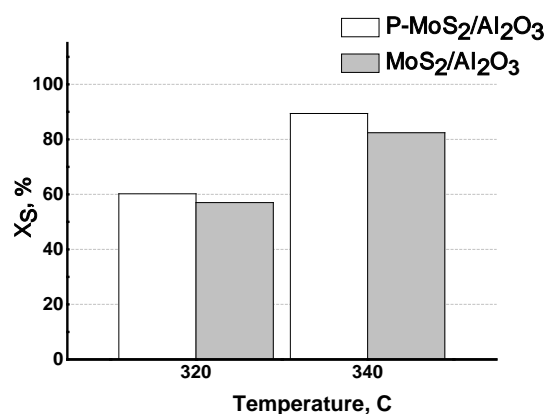
The obtained data show that  $\text{MoS}_2$  particles in the P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalyst are characterized by a lower average size of coherently scattering domain  $d_{\text{XRD}}$ . The best fitting results were obtained at the slab sizes of 2.5 and 3.2-3.5 nm for P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  and  $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalysts, respectively. A comparison of the particle sizes evaluated from XRD and HRTEM data shows a pronounced discrepancy. The dimensions of the coherent scattering domains determined from XRD data are significantly smaller than slab length of  $\text{MoS}_2$  determined from HRTEM data (Table 1). The discrepancy is explained by deformation of  $\text{MoS}_2$  particles, which leads to breaking coherence. Indeed, the  $\text{MoS}_2$  sheets observed in the HRTEM images are curved or folded (Fig. 3). A lower value of  $d_{\text{XRD}}$  in the case of P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalyst seems to result from a higher degree of deformation of the supported  $\text{MoS}_2$  particles.

The results of catalytic testing of the  $\text{MoS}_2/\text{Al}_2\text{O}_3$  and P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalysts in the hydrotreating of RSO/SRGO mixture are presented in the Fig.5-6. Degree of RSO hydrodeoxygenation (Fig.5) was

calculated using oxygen content in the raw material (mixture of RSO with SRGO) and in the liquid products measured by means of Vario EL Cube analyzer. The RSO conversion achieved 100% at 320 and 340°C over both catalysts; but P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalyst demonstrated higher HDO activity at 260, 280 and 300°C (Fig.5). P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalyst as well displayed higher activity in HDS of SRGO in comparison with  $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalyst in the whole temperature range (Fig.6).



**Fig.5.** Hydrodeoxygenation activity of P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  and  $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalysts at different temperatures



**Fig.6.** Hydrodesulfurization activity of P- $\text{MoS}_2/\text{Al}_2\text{O}_3$  and  $\text{MoS}_2/\text{Al}_2\text{O}_3$  catalysts at 320 and 340°C

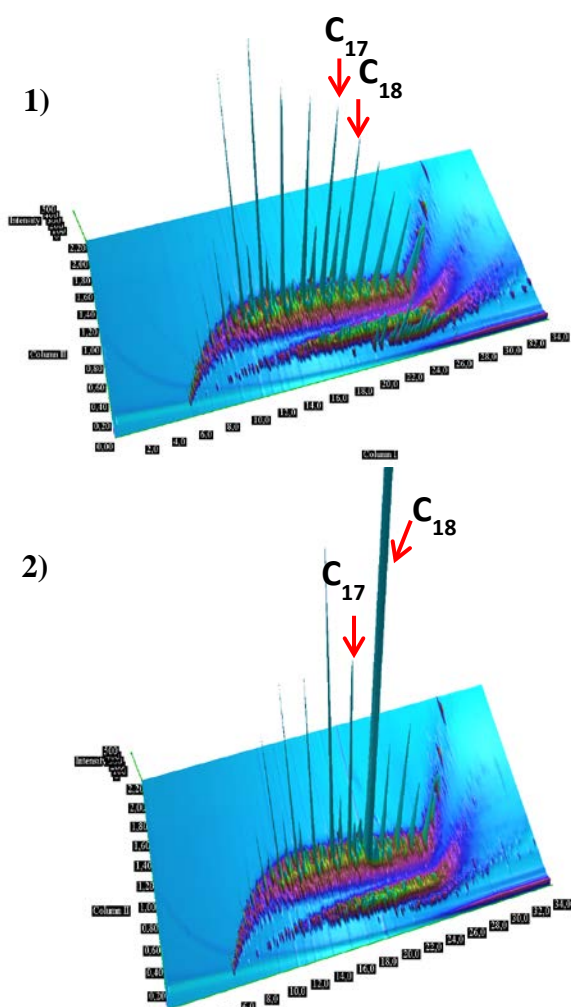
The selectivity of RSO conversion through HDO or  $\text{HDeCO}_x$  pathways was evaluated taking gas phase analysis and the results of  $\text{C}_{18}$  and  $\text{C}_{17}$  content measurement by means of two-dimensional chromatography.

The typical chromatograms of SRGO and reaction products, obtained during HDO of RSO/SRGO mixture over  $\text{MoS}_2$  at 340°C is presented in Fig.7. The quantitative analysis of  $\text{C}_{18}$  and  $\text{C}_{17}$  in the reaction products and in the SRGO let



us to calculate the selectivity of octadecane formation that lies within the region 97-99% for both catalysts at whole conversion of RSO (at 320 and 340°C).

The results of CO<sub>x</sub> analysis in the exit gas flow confirmed the high selectivity of RSO hydrodeoxygenation through the “direct” HDO route over both catalysts. CO<sub>x</sub> content was negligible at 260°C (about 0.04 vol.%) and slightly increased (up to 0.10-0.12 vol.%), with the temperature raising from 260 to 340°C. But the selectivity of DeCO<sub>x</sub> pathway calculated from the gas phase analysis did not exceed 3.0% even at 340°C.



**Fig.7.** 2D-chromatograms of straight run gas oil (1) and the product obtained (2) in presence of P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> at 340°C

## 4 Conclusion

The effect of phosphorus addition on the morphology of MoS<sub>2</sub> phase and catalytic performance of sulfide Mo/Al<sub>2</sub>O<sub>3</sub> catalysts in the HDO of rapeseed oil was studied using two different

impregnating solutions for preparation of the catalysts. MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst was obtained from solution prepared using MoO<sub>3</sub> and citric acid; the solution prepared from MoO<sub>3</sub>, citric acid and H<sub>3</sub>PO<sub>4</sub> was used for the P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst preparation. The thorough investigation of the sulfide MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> and P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts with XRD and HRTEM methods led us to conclusion, that despite nearly the same average slab length of MoS<sub>2</sub> particles determined with HRTEM on the surfaces of both catalysts, the MoS<sub>2</sub> particles in the P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts are characterized by a lower average size of coherently scattering domain d<sub>XRD</sub>. A lower value of d<sub>XRD</sub> in the case of P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst seems to result from a higher degree of deformation of the supported MoS<sub>2</sub> particles, maybe due to P incorporation in the MoS<sub>2</sub> slabs. Higher degree of deformation in turn could have been a reason of higher activity of P-MoS<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst in HDO and HDS reactions.

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## References:

- [1] Al-Sabawi M., Chen J., Hydroprocessing of biomass-derived oils and their blends with petroleum feedstocks: a review, *Energy & Fuels*, Vol.26, №9, 2012, pp. 5373-5399.
- [2] Furimsky E., Hydroprocessing challenges in biofuels production, *Catalysis Today*, Vol.217, 2013, pp. 13-56.
- [3] Kubicka D., Tucas V. *Advances in Chemical Engineering*, Elsevier, Vol.42, 2013.
- [4] Mohammad M., Hari T. K., Yaakob Z., Sharma Y. C., Sopian K., Overview on the production of paraffin based-biofuels via catalytic hydrodeoxygenation, *Renewable and Sustainable Energy Reviews*. Vol.22, 2013, pp. 121-132.
- [5] Satyarthi J.K., Chiranjeevi T., Gokak D.T., Viswanathan P.S., An overview of catalytic conversion of vegetable oils/fats into middle distillates, *Catalysis Science & Technology*, Vol.3, 2013, pp. 70-80.

- [6] Nikul'shin P., Sal'nikov V., Pimerzin A., Eremina Y., Koklyukhin A., Tsvetkov V., Pimerzin A., Co-hydrotreating of straight-run diesel fraction and vegetable oil on Co(Ni)-PMo/Al<sub>2</sub>O<sub>3</sub> catalysts, *Petroleum Chemistry*, Vol.56, №1, 2016, pp. 56-61.
- [7] Vlasova E. N., Deliy I. V., Nuzhdin A. L., Aleksandrov P. V., Gerasimov E. Y., Aleshina, G. I., Bukhtiyarova, G. A., Catalytic properties of CoMo/Al<sub>2</sub>O<sub>3</sub> sulfide catalysts in the hydrotreating of straight-run diesel fraction mixed with rapeseed oil, *Kinetics and Catalysis*, Vol.55, №4, 2014, pp. 481-491
- [8] Anthonykutty J. M., Linnekoski J. et al., Catalytic upgrading of crude tall oil into a paraffin-rich liquid, *Biomass Conversion and Biorefinery*, Vol.5, №2, 2015, pp. 149-159.
- [9] Tóth C., Baladincz P., Hancsók J, Production of biocomponent containing gas oil with the coprocessing of vegetable oil–gas oil mixture, *Topics in Catalysis*, Vol.54, №16-18, 2011, pp. 1084-1093.
- [10] Srifa A., Faungnawakij K. et al., Production of bio-hydrogenated diesel by catalytic hydrotreating of palm oil over NiMoS<sub>2</sub>/gamma-Al<sub>2</sub>O<sub>3</sub> catalyst, *Bioresource Technology*, Vol.158, 2014, pp. 81-90.
- [11] Kubicka D., Kaluza L., Deoxygenation of vegetable oils over sulfided Ni, Mo and NiMo catalysts, *Applied Catalysis A: General*, Vol.372, №2, 2010, pp. 199-208.
- [12] De Brimont M. R. et al., Deoxygenation mechanisms on Ni-promoted MoS<sub>2</sub> bulk catalysts: a combined experimental and theoretical study, *Journal of Catalysis*, Vol.286, 2012, pp. 153-164.
- [13] Deliy I. V. et al., Hydrodeoxygenation of methyl palmitate over sulfided Mo/Al<sub>2</sub>O<sub>3</sub>, CoMo/Al<sub>2</sub>O<sub>3</sub> and NiMo/Al<sub>2</sub>O<sub>3</sub> catalysts, *RSC Advances*, Vol.4, №5, 2014, pp. 2242-2250.
- [14] Debye P., Scattering from non-crystalline substances, *Ann. Physik.*, Vol. 46, 1915, pp. 809-823.
- [15] Guinier A., *X-ray Diffraction in Crystals, Imperfect Crystals and Amorphous Bodies*, Dover, New York, 1994.
- [16] Hall B. D., Debye function analysis of structure in diffraction from nanometer-sized particles, *Journal of Applied Physics*, Vol.87, №4, 2000, pp. 1666-1675.
- [17] Tsybulya S. V., Yatsenko D. A., X-ray diffraction analysis of ultradisperse systems: The Debye formula, *Journal of Structural Chemistry*, Vol.53, №1, 2012, pp. 150-165.
- [18] Yatsenko D. A., Tsybulya S. V., DIANNA (Diffraction Analysis of Nanopowders): Software for structural analysis of ultradisperse systems by X-Ray methods, *Bulletin of the Russian Academy of Sciences: Physics.*, Vol.76, №3, 2012, pp. 382-384.